Integrability of central extensions of the Poisson Lie algebra via prequantization

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June 25, 2015

Abstract

We present a geometric construction of central $S^1$-extensions of the quantomorphism group of a prequantizable symplectic manifold. This gives rise to central extensions of the universal cover of the group of Hamiltonian diffeomorphisms.

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